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Application of ground-penetrating radar technique to evaluate the waterfront location in hardened concrete

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Abstract. The long-term performance of concrete structures is directly tied to two factors: concrete durability and strength. When assessing the durability of concrete structures, the study of the water penetration is paramount, because almost all reactions like corrosion, alkali–silica, sulfate, etc., which produce their deterioration, require the presence of water. Ground-penetrating radar (GPR) has shown to be very sensitive to water variations. On this basis, the objective of this experimental study is, firstly, to analyze the correlation between the water penetration depth in concrete samples and the GPR wave parameters. To do this, the samples were immersed into water for different time intervals and the wave parameters were obtained from signals registered when the antenna was placed on the immersed surface of the samples. Secondly, a procedure has been developed to be able to determine, from those signals, the reliability in the detection and location of waterfront depths. The results have revealed that GPR may have an enormous potential in this field, because excellent agreements were found between the correlated variables. In addition, when comparing the waterfront depths calculated from GPR measurements and those visually registered after breaking the samples, we observed that they totally agreed when the waterfront was more than 4 cm depth.

environmental impacts. The traditional systems used to assess the durability of concrete structures are expensive, time consuming and, what is worse, cause damages. To overcome these drawbacks, nondestructive techniques (NDTs) are being under study to measure concrete properties that are related to durability.

The long-term performance of concrete structures can be compromised not only by poor construction practices but also, due to the permeability of concrete, by environmental agents, when they are aggressive. Since concrete is a porous material, water, containing dissolved potential deleterious substances or gases, may penetrate and be transported through the pore structure and cracks. Later on, the presence of moisture may contribute to the chemical and physical deterioration of the concrete. In particular, for much pathology, the common catalyst is moisture, since all chemical reactions (corrosion, alkali–silica, sulfate, etc.) need some water to develop (Klysz et al., 2008). Therefore, the analysis of water penetration in concrete is critical when durability studies are performed (Otieno et al., 2010).

Currently there are several NDTs available to evaluate the condition of structures from the effects of moisture penetration. Tosti and Slob (2015) give a quick review about those methods and highlight the big potential of ground-penetrating radar (GPR).

GPR is based on the emission and reception of electromagnetic waves. The propagation velocity of these waves through a body is governed by the dielectric permittivity of its material. Since water has the highest dielectric permittivity, the water content variations in the concrete produce variations in the dielectric permittivity of concrete and, consequently, in the wave parameters (Soutsos et al., 2001; Lai

1 Introduction

Concrete is the most used man-made construction material around the world. For this reason, the durability of the concrete structures plays an important role when trying to avoid repairs and replacements, which in turn reduces costs and

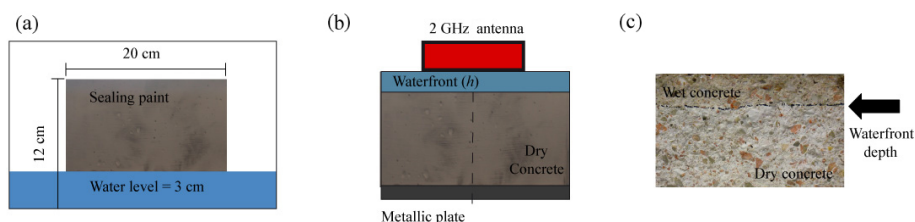


Figure 1. (a) Concrete samples immersed into 3 cm of water; (b) GPR acquisition procedure; (c) waterfront marked in the sample after conducting GPR measurements and breaking the sample.

et al., 2009). Previous studies have reported the effect of water content on wave parameters. Some of them (Laurens et al., 2005; Sbartaï et al., 2006; Klysz and Balayssac, 2007; Martínez-Sala et al., 2013) have shown the suitability of the direct signal attenuation to characterize water content in concrete. Other works analyze the influence of water content on waves energy (Martínez-Sala et al., 2015) and models have been developed to prove a strong correlation between radar amplitude attenuation and the moisture content (Senin and Hamid, 2015; Klysz et al., 2008). A review about the techniques based on time domain and frequency on radar signals is provided by Tosti and Slob (2015). However, as far as we know, the studies carried out by Rodríguez-Abad et al. (2014, 2016a) are the only ones that deal with the assessment of the location and determination of the waterfront depth from electromagnetic wave parameters.

In line with this former investigation, the aim of this paper is to analyze the effect of differential waterfront depths on the wave velocity and find out the waterfront depth in concrete specimens, which have been partially immersed in water. While the study of Rodríguez-Abad et al. (2016a) was conducted placing the GPR on the surface opposite the immersed one, in this case, the study was performed by placing the GPR antenna on the same surface that was immersed into water, the preliminary analysis of which was presented in the European Geosciences Union (EGU) General Assembly (Rodríguez-Abad et al., 2016b). To carry out these two studies, 24 concrete specimens were fabricated, cured and dried in a kiln. After being partially immersed in water during different time intervals, for the present work, GPR measurements were conducted on the wet face of the samples by using a 2 GHz antenna. Finally, the samples were broken to visually measure the actual waterfront depth.

2 Material and method

The experimental program was conducted on ordinary concrete samples made with water/cement ratio of 0.65, manufactured with a CEM I 52,5 R/SR cement. A total of 24 concrete samples measuring $0.20 \times 0.20 \times 0.12 \text{ m}^3$ were fabricated. The samples were cured by immersion in a wet chamber for a period of 28 days, in accordance with the stan-

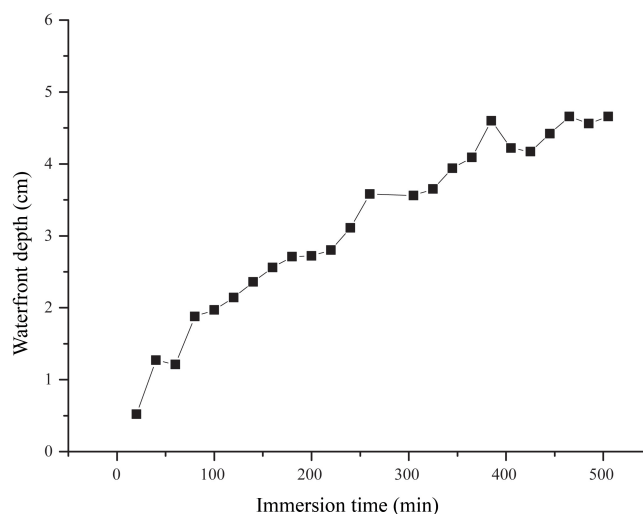


Figure 2. Waterfront depth advance in time.

dard (UNE-EN 12390-2:2009). After that, they were left to conduct the curing process under atmospheric conditions up to 90 days. With this age the samples were introduced in a kiln (105°C) to dry them completely. Subsequently, the samples were taken out of the kiln and sealing paint was applied on all surfaces, except for the ones that would be in contact with water and the opposite side. Finally, samples were immersed into 3 cm of water (Fig. 1a).

The GPR measurements were performed before and after submerging the samples. Finally, all specimens were broken in two parts and the correct positions of the waterfronts were marked and measured. The final waterfront values are depicted in Fig. 2. By means of the visual inspection, it could be clearly observed that the distribution consisted of a saturated zone and a drier zone (Fig. 1c).

GPR measurements were carried out using a SIR-3000 system with a 2 GHz ground coupled antenna (GSSI). The GPR measurements consisted in recording 400 static traces by placing the antenna on the center of the surface immersed in water. In order to enhance the reflected waveforms, a metallic reflector plate was placed beneath all the samples (Fig. 1b).

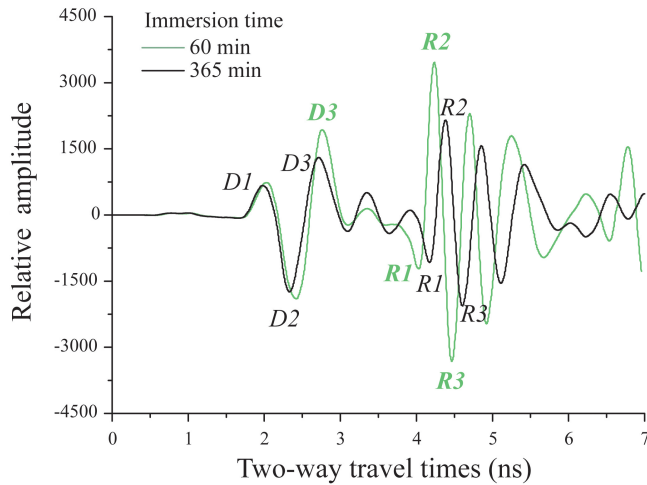


Figure 3. Effect of water immersion on reflected peaks.

3 Results and discussion

3.1 Effect of water content on direct and reflected wave GPR signals

Prior to performing any measurements in the GPR signals, it was necessary to understand the received signals. They were composed by two parts: the direct wave, considering this one as the overlap between the air wave and the direct wave, and the reflected wave at the bottom of the samples. Both of them were composed by three main peaks, respectively (D1, D2, D3, R1, R2, R3) and were affected by the water immersion (Fig. 3).

To calculate the propagation velocities, it was necessary to measure the arrival times in GPR signals. However, due to the interference and the attenuation of the waves, it was difficult to identify which maximum was representative of the wave arrival. To overcome this difficulty, velocities were calculated with all the peaks combinations in order to know which one provided better agreement with the waterfront depth. For each sample and peak combination, the velocity was calculated with the following equation:

$$v = \frac{2l}{\Delta t_D^R} = \frac{\left(2\sqrt{H^2 + \left(\frac{d_0}{2}\right)^2}\right)}{\Delta t_D^R}, \quad (1)$$

where l was the half of the path the wave traveled, Δt_D^R was the arrival time increment between the reflected and direct wave, d_0 was the distance between emitter and receiver (4 cm) and H the width of the sample (12 cm). Finally, the velocity difference, when the sample was dry and wet, was determined by Eq. (2):

$$\Delta v \left(\frac{\text{cm}}{\text{ns}} \right) = v_{\text{im}} - v_{\text{d}}, \quad (2)$$

Table 1. Waterfront advance depth in centimeters and best adjustments with velocity increments.

Peaks combination	Second-order polynomial fit $y(x) = ax^2 + bx + c$			
	a	b	c	R^2
R1-D1	6×10^{-7}	-0.04	0.09	0.99
R1-D2	0.0002	0.07	0.81	0.81
R1-D3	0.001	0.13	1.75	0.62
R2-D1	-8×10^{-5}	-0.03	0.02	0.99
R2-D2	4×10^{-5}	-0.05	0.56	0.97
R2-D3	6×10^{-4}	-0.09	1.19	0.67
R3-D1	2×10^{-4}	-0.03	0.06	0.97
R3-D2	4×10^{-5}	-0.05	0.49	0.94
R3-D3	9×10^{-4}	-0.09	0.95	0.58

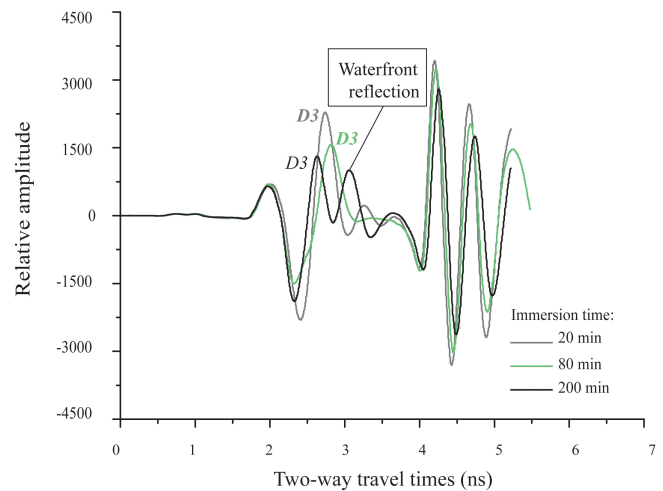


Figure 4. Overlap between peak D3 of direct wave and waterfront reflection.

where v_{im} was the wave velocity when the sample was immersed into water and v_{d} was the velocity when the sample was dry.

In addition, velocity increments were correlated with the waterfront depths in order to check which one provided a better agreement between both parameters. The results of which are summarized in Table 1.

The results show a good agreement between velocity increments and waterfront depth for all peaks combinations, except for the ones that were calculated with peak D3. This result was expected, since D3 was a peak affected by two signals: the direct wave and the reflection of the waterfront. It is not after 325 min of immersion that the waterfront reflection was totally separated from the direct wave (Fig. 4).

It is important to highlight the consequence of these results, because even if we were not able to locate the waterfront reflection or if it were overlapped with the direct wave signal, we might predict the waterfront position with high re-

Table 2. Theoretical vertical resolution, considering the different peaks combinations to calculate velocities.

	Peaks considered to calculate velocities								
	R1–D1	R1–D2	R1–D3	R2–D1	R2–D2	R2–D3	R3–D1	R3–D2	R3–D3
Samples immersion time	Velocities (cm ns ⁻¹)								
Dry: 0 min	12.45	14.71	17.98	11.41	13.28	15.89	10.29	11.79	13.80
After immersion: 505 min	11.05	13.18	16.48	10.05	11.79	14.35	9.27	10.72	12.80
	Vertical resolution (cm)								
Dry: 0 min	3.11	3.68	4.49	2.85	3.32	3.97	2.57	2.95	3.45
After immersion: 505 min	2.76	3.30	4.12	2.51	2.95	3.59	2.32	2.68	3.20

liability, regardless of the peaks combination used, except for D3. In particular, the peaks combination of D1–R1 used to calculate the velocity increment presented an excellent correlation, as can be observed in Fig. 5.

3.2 Effect of waterfront reflection on GPR signals

The next step was to process the waterfront reflection. According to Pérez Gracia (2001) the vertical resolution (R_v) is calculated by the following equation:

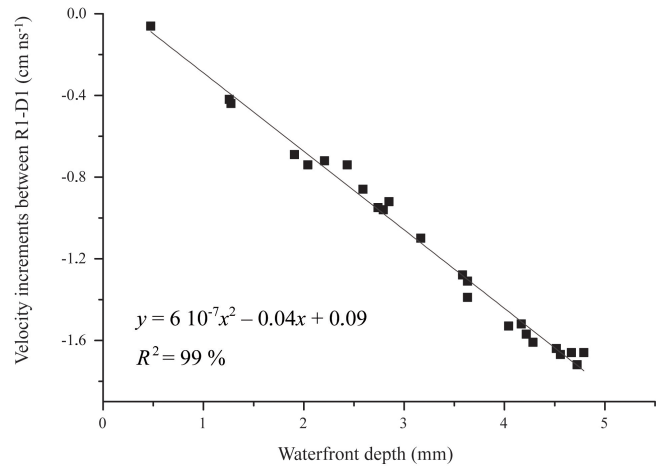
$$R_v = \frac{v}{2f}, \quad (3)$$

where v is the wave velocity and f is the wave frequency. In Table 2 the extreme velocity values and vertical resolution are presented, which ranged from 2.3 to 4.5 cm. This means that interfaces located under these distances might not be identifiable. Nevertheless, the following analysis was conducted to check the reliability of this statement.

The waterfront reflection was composed of three maximums (F1, F2 and F3), but they were only identifiable after a long period immersed in water (465 min), as it can be observed in Fig. 6. Only after 325 min of immersion, the waterfront reflection was not overlapped with the direct wave and as the waterfront depth increased its signal become more easily identifiable. Nevertheless, in all cases the peak F3 was reliably identifiable; therefore, it was used as the waterfront reflection arrival in the following calculations.

In order to check the reliability of the waterfront identification, a regression linear analysis was used to find the relationship between the arrival times of the direct and reflected peaks and the waterfront peaks. As it can be observed in Fig. 7, an excellent agreement was found between peak D2 of the direct wave and F3 of the waterfront reflection. Likewise, excellent results were found when relating peak R3 of the reflected wave and F3 of the waterfront.

These results are of great importance, because that means that the GPR technique working with a commercial antenna of 2 GHz central frequency had enough sensitivity to detect a waterfront that ranged from 0.5 to 4.7 cm and this limit was far beyond the theoretical vertical resolution (Table 2).

**Figure 5.** Velocity increments calculated with the peaks combination D1–R1 versus waterfront depth.

3.3 Waterfront depth assessment

The final step was to assess the capability of GPR signals to determine the waterfront depth. Although there is refraction at the interface between dry and wet concrete, in this work we use a simpler model. Due to the small sample size, the short distances of the propagation paths and the refraction angle changes, we consider them to be neglected. Considering this approach, this model is depicted in Fig. 8. Analyzing propagation paths, arrival time increments at the different interfaces reflections were able to be calculated. The equations of these time increments were

$$[(\Delta t)_{D2}^{R1}]_{\text{wet}} = 2 \left(\frac{l_1}{v_{\text{wet}}} + \frac{l_2}{v_{\text{dry}}} \right) - \frac{d_0}{v_{\text{wet}}}, \quad (4)$$

$$[(\Delta t)_{F3}^{R3}]_{\text{wet}} = 2 \left(\frac{l_1}{v_{\text{wet}}} + \frac{l_2}{v_{\text{dry}}} - \frac{l_3}{v_{\text{wet}}} \right), \quad (5)$$

where $[(\Delta t)_{D2}^{R1}]_{\text{wet}}$ were arrival time increments between direct and reflected at the bottom of samples waves and $[(\Delta t)_{F3}^{R3}]_{\text{wet}}$ were arrival time increments between waterfront reflections and reflections at sample bottoms. Both values

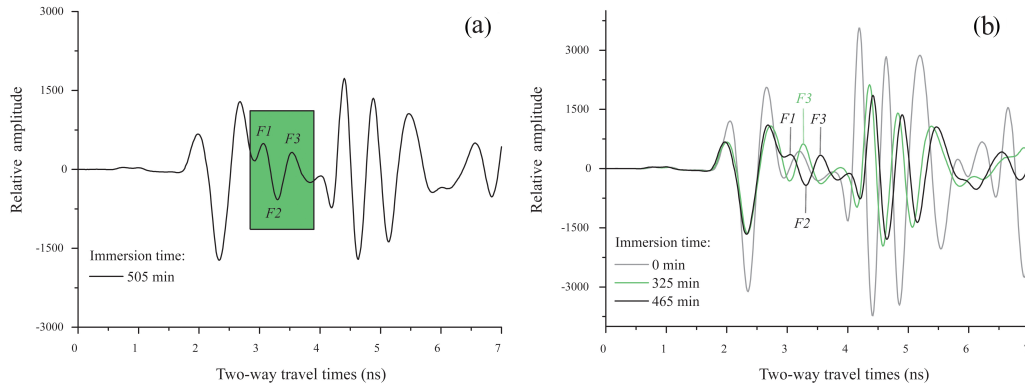


Figure 6. (a) Waterfront reflection maximum peaks; (b) waterfront reflection evolution along immersion time.

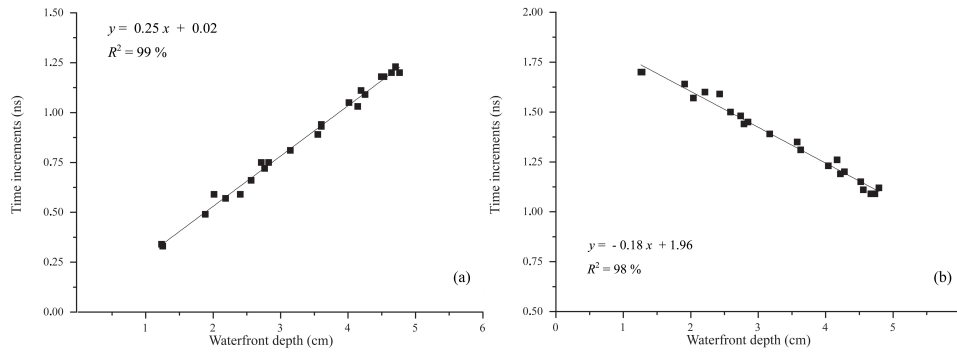


Figure 7. (a) Adjustments of the arrival time increment between D2 and waterfront reflection (F3) and waterfront depths; (b) arrival time increment between R3 and waterfront reflection (F3) and waterfront depths.

were possible to be measured in the GPR signals. Likewise, v_{dry} , which corresponds to the velocity of the GPR signals along the dry part of samples, was calculable from the GPR signals by means of the following equation:

$$v_{\text{dry}} = \frac{\left(2\sqrt{H^2 + \left(\frac{d_0}{2}\right)^2}\right)}{(\Delta t_{\text{D2}}^{\text{R1}})_{\text{dry}}}, \quad (6)$$

where $(\Delta t_{\text{D2}}^{\text{R1}})_{\text{dry}}$ was the arrival time increments between reflected and direct waves when samples were dry, d_0 was the distance between emitter and receiver and H the width of the sample. In addition, the half of the paths that each wave traveled, that is l , l_1 , l_2 and l_3 (Fig. 8), could be calculated as follows:

$$l = \sqrt{\left(\frac{d_0}{2}\right)^2 + H^2}, \quad (7)$$

$$l_1 = \frac{h}{H}l, \quad (8)$$

$$l_2 = \frac{H-h}{H}l, \quad (9)$$

$$l_3 = \sqrt{\left(\frac{d_0}{2}\right)^2 + h^2}, \quad (10)$$

where h was the unknown value to be determined: waterfront depth. Substituting Eqs. (6), (7), (8), (9) and (10) in Eqs. (4) and (5), we had two equations with two unknowns: waterfront depth and velocity in the wet part of the sample (v_{wet}). The v_{wet} was assumed to be constant, since the absorption coefficient of the wet zone remained quite stable (Average C_A wet zone = 4.5 %), regardless of the height of the waterfront.

After solving these two nonlinear equations system, the waterfront was determined. The solution did not converge for the first 325 min of immersion. This was expected, since some generalizations were assumed when calculating the propagation paths and, in addition, the waterfront depths of these samples were on the range of the antenna resolution. Nevertheless, very interesting results were obtained for the samples that remained immersed more than 345 min. The waterfront depths obtained after breaking the samples and the ones calculated by the procedure explained above are detailed in Table 3.

This means that with a GPR commercial antenna of 2 GHz central frequency and placing it on the side which had been

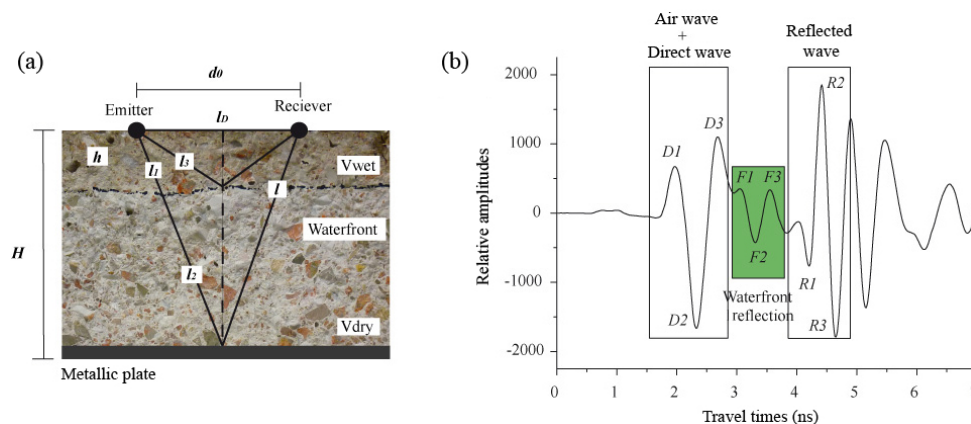


Figure 8. (a) Sketch of the propagation paths model; (b) typical GPR signal acquired when the sample was immersed.

Table 3. Waterfront determination by means of GPR signals.

Sample immersion time	Waterfront depth (cm)		Difference (cm)
	After breaking samples	GPR signals	
345	4.04	3.35	0.69
365	4.17	–	–
385	4.79	4.50	0.29
405	4.22	3.95	0.27
425	4.28	3.85	0.43
445	4.52	4.35	0.17
465	4.73	4.65	0.07
485	4.56	4.70	–0.14
505	4.67	4.75	–0.08

in contact with water, waterfront depths could be calculated quite accurately, but only when the waterfront had a height bigger than 4 cm.

4 Conclusions

Concrete durability depends mainly on its permeability. Therefore, the analysis of water penetration in concrete is critical when durability studies are performed. This research analyzed the capability of the GPR technique to evaluate the location of the waterfront by means of a commercial antenna of 2 GHz central frequency, when the GPR data were acquired placing the antenna on the surface of the concrete specimen which was immersed into water. The election of this antenna display was based on the idea that this will be probably the only possible acquisition procedure when studying concrete structures in service.

It was found that direct and reflected waves at the samples bottom were greatly affected by the waterfront advance, since they described with great approximation the waterfront

increment. It is very important to highlight that it was not necessary to locate the waterfront reflection to find great correlations between these parameters ($R^2 = 99\%$). In addition, despite the fact that the waterfront height was smaller than the vertical resolution, the location of the waterfront reflection was possible after analyzing the GPR signals. Indeed, it was possible to detect the waterfront arrival, even in those cases in which the waterfront was overlapped with the direct wave, as it was proven by the high correlation coefficients found ($R^2 = 99\%$). Finally, a special procedure was developed to calculate the waterfront position. In this case, the results proved that by using the simplified model of the propagation paths used in this work, it was possible to assess the waterfront depth, although only when it was greater than 4 cm.

For all these reasons, it can be concluded that the GPR is a powerful technique to assess and locate the waterfront advance in hardened concrete when using a 2 GHz commercial antenna. However, further research will be needed with a larger number of samples, with a variety of dimensions and different water/cement ratios and different frequency antennas.

5 Data availability

The data sets are available in Excel format as the Supplement. In the first file, the raw signals acquired by GPR are included (DATA SETS Raw signals.xls). In this file, each column corresponds to one of the 24 concrete samples analyzed scans. For all samples the column order is always the same: firstly the scan acquired when the sample was immersed into water and secondly the scan obtained before immersion. In the second file (DATA SETS-Waterfront depth-Visual.xls), the depth of the waterfront advance, obtained by visual inspection after breaking the samples, for the 24 concrete samples is detailed.

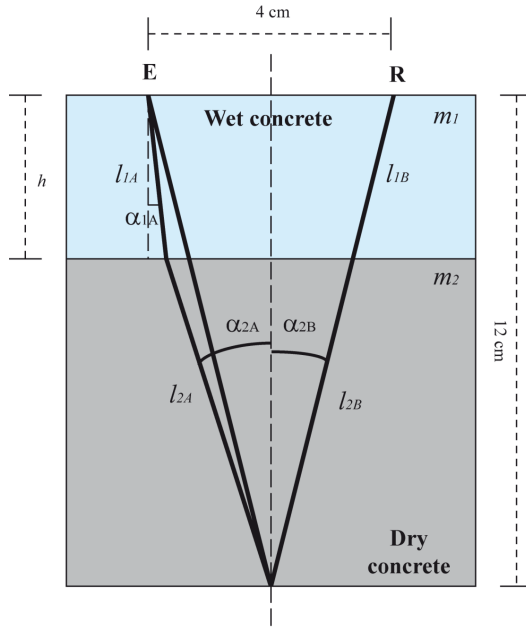


Figure A1. Electromagnetic traveling paths models.

Appendix A: Justification of the approximations of the electromagnetic modeling

In Fig. A1, electromagnetic modeling (EM modelling A) that takes into account the bending of the propagation paths and the electromagnetic modeling used in this paper (EM model B) can be observed. The EM model B considers some approximations and their validity was justified by the following calculations.

The first step to validate EM model B was its definition. As depicted in Fig. A1, there were two media that corresponded to the wet (m_1) and dry concrete (m_2). EM model B considered that there was no change in the propagation paths. Therefore, l_{1B} and l_{2B} was assumed to be a single line. The second step was to calculate the length of l_{1B} and l_{2B} . According to the dimensions of the concrete samples and the distance between emitter and receiver of the 2 GHz antenna manufactured by GSSI, the reflection angle in this model (α_{2B}) was calculated as follows:

$$\alpha_{2B} = \arctg\left(\frac{2}{12}\right) = 9.46^\circ. \quad (\text{A1})$$

For the most unfavorable case, that is, when the waterfront was deepest, the waterfront depth (h) when the sample was broken was found to be $h = 4.70$ cm (Table 3). Then, l_{1B} and l_{2B} were calculated with Eqs. (12) and (13).

$$l_{1B} = \frac{h}{\cos\alpha_{2B}} = 4.76 \text{ cm} \quad (\text{A2})$$

$$l_{2B} = \frac{12 - h}{\cos\alpha_{2B}} = 7.40 \text{ cm} \quad (\text{A3})$$

The third step was to calculate the length of the travel paths considering EM model A (l_{1A} and l_{2A}). According to Snell's law and the geometry of the problem (Fig. A1), we obtained two equations with two unknowns:

$$\frac{v_2}{v_1} = \frac{\sin\alpha_{2A}}{\sin\alpha_{1A}}, \quad (\text{A4})$$

$$(12 - h) \cdot \tan\alpha_{2A} + h \cdot \tan\alpha_{1A} = 2. \quad (\text{A5})$$

To solve Eqs. (14) and (15), the most unfavorable case ($h = 4.70$ cm) was considered, in which the resulting velocities when solving the Eqs. (6) and (4) for this sample were propagation velocity when the wave traveled along the wet part, $v_1 = (v_{\text{wet}})_{D2}^{\text{R1}} = 8.18 \text{ cm ns}^{-1}$, and when traveled along the dry part, $v_2 = (v_{\text{dry}})_{D2}^{\text{R1}} = 12.40 \text{ cm ns}^{-1}$. Finally, the refraction angles were found to be $\alpha_{1A} = 7.18^\circ$ and $\alpha_{2A} = 10.92^\circ$ and the paths l_{1A} and l_{2A} were calculated with Eqs. (16) and (17).

$$l_{1A} = \frac{h}{\cos\alpha_{1A}} = 4.74 \text{ cm} \quad (\text{A6})$$

$$l_{2A} = \frac{12 - h}{\cos\alpha_{2A}} = 7.43 \text{ cm} \quad (\text{A7})$$

The differences in the length paths between the two EM models were found to be 0.02 and 0.03 cm, respectively. The validity of the use of EM model B was confirmed, when comparing the former differences with the obtained standard deviation ($\sigma = 0.25$ cm) of the h assessment for the case under study ($h = 4.70$ cm), when the sample was broken and its depth measured by means of visual inspection, since this h was calculated by averaging 12 measuring points of the waterfront line.

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