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► To cite this version:

Narintsoa Ranaivomanana, Stéphane Multon, Anaclet Turatsinze. Tensile, compressive and flexural basic creep of concrete at different stress levels. *Cement and Concrete Research*, 2013, 52, pp.1-10. 10.1016/j.cemconres.2013.05.001 . hal-01724653

HAL Id: hal-01724653

<https://hal.insa-toulouse.fr/hal-01724653>

Submitted on 23 Mar 2018

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1 **Tensile, compressive and flexural basic creep of concrete at**
2 **different stress levels**

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8
9
10 **Abstract**

11 Concrete is brittle and highly sensitive to cracking, which is detrimental to the sustainability
12 of its applications. Although it is well known that cracks occur mainly in tension, research on
13 the mechanical behaviour of concrete is usually limited to compression and investigations of
14 creep behaviour, a major concern for concrete structures, are no exception in this respect. This
15 paper is intended to help remedy the situation. First, the new experimental set-ups developed
16 to achieve tensile and bending creep are presented. The precautions taken to obtain relevant
17 experimentation are also described. Results for specimens subjected to sustained stresses of
18 30, 40 and 50% of the tensile or compressive strength are then presented. The final discussion
19 compares basic creep under the different types of loading for the three stress levels.

20
21 **Keywords:** concrete, basic creep, shrinkage, damage, compression, tension, bending

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24 **I Introduction**

25 Concrete is brittle and highly sensitive to cracking. Its poor strain capacity and low tensile
26 strength have negative impacts on the lifetime of concrete structures. Besides, its mechanical
27 properties in tension are non-negligible for the design of concrete structures. Corres-Peiretti
28 and Caldentey [1] summarize the designer's point of view with regards to tensile strength
29 considerations in two points: the stiffening effect (which limits deflections of reinforced
30 concrete members due to the tensile capacity of the material) and the risk of brittle failure
31 (which leads to the minimum reinforcement required in concrete structures). Because of the
32 possible interaction between delayed behaviour (creep and relaxation) and damage, the former
33 has to be perfectly understood in order to evaluate the risk of cracking in concrete elements.
34 Stresses induced by shrinkage can be relaxed of more than 50% due to tensile creep which
35 can thus hinder crack formation according to Altoubat and Lange [2]. However, it does not
36 mean that cracking is totally stopped by such relaxation phenomenon. Actually microcracks
37 can still propagate even if the external load decreased due to stresses relaxation, mostly for
38 high stress levels at which viscoelastic behaviour of concrete becomes non-linear [3]. The final
39 aim of this paper is to improve knowledge of tensile creep in concrete by comparing basic
40 creep in tension, basic creep in flexure and basic creep in compression at different loading
41 levels.

42 **II Literature review**

43 Tensile tests on cement-based materials are not easy to perform because the material is brittle
44 and the strains are small, thus difficult for most extensometers to measure accurately [4]. How
45 to fix the samples to the loading device [5] is also an important issue. For all these reasons,
46 very few studies have been devoted to tensile creep of concrete. Most tensile creep
47 experiments on cement-based materials have been performed at early age [6, 7] and even at
48 very early age, just a few hours after casting [8–11]. During this period, concrete undergoes
49 large dimensional changes, induced by hydration reactions (Le Chatelier contraction), drying
50 and thermal variations in the case of massive elements, which generally result in a net
51 contraction (shrinkage) of the material. Depending on ambient conditions, the magnitude of
52 the shrinkage strain may reach high values (500 to 1000 $\mu\text{m}/\text{m}$ at 50% RH [12]), much greater
53 than the elastic deformation (about 100 to 200 $\mu\text{m}/\text{m}$ [12]). It is necessary however to take
54 into account the viscoelastic strain components when considering the actual state of stress,
55 especially in the case of partially or fully restrained shrinkage [13, 14]. Some investigations

56 on tensile creep of concrete at early age have addressed the effects of various parameters
57 (W/C ratio, stress level, etc.) on the time-dependent strain magnitude and kinetics. In some
58 others, creep in direct tension and creep in compression were compared [15, 16], bringing to
59 light similarities as well as differences. Concerning similarities, at early age, the tensile and
60 compressive creep rates are very large, but decrease sharply over time. The ageing effect
61 appears to be very significant, especially during the first few days after casting. As for
62 differences, Atrushi [16] has pointed out that compressive creep is higher than tensile creep
63 just after loading. But, as the phenomenon stabilizes more quickly in compression, the
64 amplitude of tensile creep becomes higher a few days later. These results are, however, in
65 contradiction with Illston's findings [15] which reveal an opposite trend.

66 As the aforementioned tests were carried out a short time after casting, the coupling between
67 creep and the effects of hydration (increase in strength and stiffness, shrinkage, etc.) remained
68 very strong [9] and the results obtained could be different in the case of older concrete.
69 Accordingly, in the model proposed by De Schutter for basic compressive creep at early age,
70 the degree of hydration at loading becomes an important parameter influencing the strain
71 evolution as well as its final value [17]. Tensile creep data for cement-based materials older
72 than 28 days, i.e. when hydration reactions are almost stabilized, are rare. Based on the few
73 reported studies, tensile creep experiments on mature concrete have also dealt with basic
74 aspects as the concrete composition and the stress level [18–20] and the comparison between
75 tension and compression behaviours [21–23]. A fundamental feature that differentiates tensile
76 creep from compressive creep is that, for a fully dried concrete, compressive creep is almost
77 negligible [24, 25] while tensile creep remains significant [26]. These findings suggest that
78 the two delayed strains may result from different mechanisms such that further comparative
79 studies could be instrumental in gaining a better understanding of tensile creep. One of the
80 most relevant studies dealing with this aspect is that performed by Brooks and Neville at the
81 University of Leeds in 1977 [21]. According to these authors, basic creep in tension and basic
82 creep in compression are similar during the first 20 days of loading. After 40 days, strain
83 variations measured on the specimens in compression slow down while opposite trend is
84 observed for strain variations measured on the specimens in tension. Thus the creep behaviour
85 seems to deviate in tertiary after 60 days of loading in tension. Findings for total creep (basic
86 creep + drying creeps) were quite different: total tensile creep and compressive creep appear
87 to behave similarly after two or three days of loading. Recent studies [22, 23] reveal that
88 compressive basic creep is two to three times larger than tensile basic creep, which is in

89 contradiction with the results obtained by Brooks and Neville. However, the rare available
90 experimental data have to be interpreted carefully, especially when considering the difficulty
91 inherent to the measurement of really small strains and the potentially quite different
92 experimental conditions involved in the various studies. For instance, the extensometers used
93 for strain measurements were not the same (embedded acoustic gauge for Brooks and Neville
94 [21] and LVDT transducers fixed on the specimen for Reviron et al. [22] and Rossi et al.
95 [23]). As for the test conditions, the term autogenous used by Brooks and Neville [21]
96 actually corresponded to a test involving immersion in water. It is worth mentioning that
97 tensile creep appears to be practically irreversible [19, 21], unlike compressive creep.

98 Finally, although all authors agree on the existence of a stress threshold beyond which the
99 behaviour can change dramatically in tertiary creep and cause the failure of the specimen in
100 tension without any further increase in applied load, the limit value is not well established.
101 Depending on the authors, this threshold would reach about 40% and 85% of the average
102 strength for concrete cured in water and between 60% and 90% for autogenous curing
103 conditions [18, 27-28]. Therefore, during this study, tests were not carried out at stress levels
104 higher than 50% of the ultimate stress beyond which, according to Pigeon and Bissonnette
105 [29], the relation between creep and stress probably becomes non-linear and time-dependent
106 failure is possible.

107 In summary, tensile creep data for concrete loaded more than 28 days after casting, notably
108 sound comparisons with compressive creep, are scarce in the literature. This paper presents
109 the results of a comparative study focusing on creep in direct tension, creep in direct
110 compression and creep in flexure and intended to improve the understanding of the delayed
111 behaviour of concrete subjected to creep in flexure sustained loading. Three stress levels
112 assumed to fall within the linear creep regime were chosen: 30%, 40% and 50%. The
113 experimental set-ups developed to achieve these tests are described hereafter. Then,
114 experimental shrinkage and creep are presented and analysed with a special emphasis towards
115 correlations and coupling between the various phenomena.

116 **III Materials and methods**

117 **III.1 Material characterization**

118 A High Performance Concrete developed for Andra (French Agency for Nuclear Waste
119 Management) for deep storage of nuclear wastes was used in this study. Its mix proportions

120 are given in Table 1. Six batches were cast: three batches for compressive creep tests and
121 three other for tensile creep tests (in direct tension and in bending). The strength and Young's
122 modulus in compression were measured for the six batches: the average values are
123 respectively 69.7 MPa and 41,925 MPa with a dispersion of about 5%. The direct tensile
124 strength was only measured for the three batches used for the tensile creep and the flexural
125 creep tests. Table 2 shows the mean values measured for direct tensile strength, direct
126 compressive strength and modulus in compression at 28 days for the three batches used for
127 the tensile creep and flexural creep tests (first three lines) and the overall average 28-days
128 value (last line), along with the corresponding coefficients of variation and the numbers of
129 samples tested. For each batch (B-30%, B-40% and B-50% stand for the three loading levels:
130 30, 40 and 50% of the mean tensile strength respectively - Table 2), a series of mechanical
131 characterization tests in direct tension and in compression were performed in order to obtain a
132 precise value of the strength of the batch used for each creep test. As can be seen, direct
133 tensile strength data exhibit a larger dispersion than compressive strength data. From a
134 statistical point of view, there is a smaller dependence of the ultimate stress on local defects in
135 compression than in tension. Because of the scatter characterizing tensile strength results, the
136 effective stress level can differ significantly from the desired value, which can lead to very
137 different results in terms of creep, particularly at high stress levels [28].

138 After demoulding, all the specimens dedicated to instantaneous mechanical tests at 28 days
139 and to creep tests were kept in water for 15 days in order to prevent the specimens from self-
140 desiccation. Then they were dried superficially and covered with triple layers of self-adhesive
141 aluminium foil, a procedure that has proven to be effective for moist-proof sealing [30].
142 Finally, the specimens devoted to creep tests were equipped with extensometers for strain
143 measurement and were stored in the test room in a controlled atmosphere (temperature: 20°C,
144 relative humidity 50%) until loading at 28 days.

145 Shrinkage and creep occur simultaneously, the common practice for many years has been to
146 consider the two phenomena as additive, which is appropriate for many practical applications
147 [32, 33]. Actually, they are not independent and the principle of superposition cannot
148 rigorously be applied. Tensile creep strains are low and are of the same order of magnitude as
149 additional strains (autogenous shrinkage, thermal strain, etc.) [34]. By assuming the effects of
150 autogenous shrinkage to be significantly reduced beyond 28 days, the principle of
151 superposition could be applied provided that some precautions are taken, particularly an
152 accurate assessment of shrinkage strain. For this purpose, strain measurements were

153 performed on non-loaded companion specimens having the same shape and size as the loaded
154 specimens. Deformations of the specimens were monitored over a long period of time using
155 long-service-life strain gauges, 60 mm in length and equipped with a stainless steel metallic
156 support that provides resistance to capillary water rise. Special glue allowed firm and durable
157 contact between the specimen and the strain gauge.

158 Autogenous shrinkage results obtained for three different batches (batches 1, 2 and 3 in Figure
159 1, corresponding to creep levels at 30, 40 and 50% of the concrete tensile strength) and for
160 two different specimen sizes (specimens 1 were 70×70×280 mm prisms and specimens 2 were
161 100×100×500 mm prisms) are reported in Figure 1. As expected, shrinkage strain values were
162 low and did not exceed 20 µm/m after 80 days of measurement. When the measurement
163 accuracy was taken into account, results indicated a low dispersion among specimens, either
164 from the same batch or from different batches. During this experimentation, it has been
165 verified that the use of three aluminium layers prevented mass loss (no mass variation was
166 detected during the first 100 days; the weighing scale resolution was of 1 g for mass higher
167 than 3 kg).

168 **III.2 Creep devices**

- 169 • Compressive creep test apparatus

170 The experimental device, the loading process, and the specimens have been described in
171 detail by Munoz [35] and Ladaoui [36]. Compressive creep devices are equipped with
172 hydraulic jacks. Each one allows simultaneous loading of 2 specimens. Longitudinal
173 deformations are recorded by means of inductive transducers located within a reservation
174 created during casting by placing a removable metallic insert in the mould axis. The central
175 steel rod (along the central axis of the specimen, Figure 2) is fixed to the lower part of the
176 specimen by a steel nut embedded in the concrete during casting. The LVDT sensor is fixed to
177 the upper part of the specimen. The displacement of the magnetic core located on the steel rod
178 provides the deformation of the specimen which was measured on a base length of 115 mm.
179 Previous studies [35] showed that the strain measurement uncertainty is equal to 9 µm/m and
180 that the difference with an external measurement (on three lines on the surface of the
181 specimen) was lower than 5%. The loading and strain measurements were performed in
182 accordance with the RILEM recommendations [37].

183

184 • Tensile creep test apparatus

185 A schematic description of the tensile creep test apparatus is given in Figure 3. The tensile
186 creep test set-up was a rigid frame with a hinged lever arm (① in Figure 3). The lever arm
187 ratio was 5/1. A 70×70×280 mm prismatic specimen ② was loaded by using calibrated
188 weights stacked on a platen ③. The load was transmitted to the specimen through a cable, one
189 end of which was welded to a steel cap glued on one side of the specimen while the other end
190 was hinged to the frame ④. A screw system located at the bottom of the rig ⑤ allowed the
191 horizontality of the lever arm to be controlled. A stopping device located below the lever arm
192 (⑥ in Figure 3) prevented sudden fall of the weights in case of failure of the loaded
193 specimen. Due to the sensitivity of tensile creep to temperature changes, all the experiments
194 were performed in a test room where temperature and RH were controlled. During the test,
195 additional precautions were taken: two specimens, one loaded to measure tensile creep and
196 the other unloaded (control specimen) to measure shrinkage strain, were positioned side by
197 side in a thermally insulated box and so had the same thermo-hygrometric history. One of the
198 difficulties with tensile tests on cement-based materials is the load transfer between the
199 specimen and the loading device [5]. In this study, the solution of gluing specimens with
200 methacrylate adhesive was opted for. The connection between the cable and the loading frame
201 was achieved with a cylindrical roller ⑦. It is worth mentioning that the use of flexible cable
202 instead of rigid attachments significantly reduced parasite bending effects in the specimen.
203 The same long-service-life gauges (60 mm in length) than for shrinkage strain measurements
204 were used for the specimens in tension.

205 • Flexural creep test apparatus

206 The flexural creep apparatus (Figure 4) was similar in principle to the oedometric device
207 used in soil mechanics. In this case, the soil specimen was replaced by prismatic concrete
208 specimens. The load was applied, as in the case of tension, by means of calibrated weights
209 stacked on a platen (① in Figure 4) fixed to a hinged lever arm ②. The lever arm ratio was
210 also 5/1. Through I-shape steel beams equipped with two metal rollers acting as simple
211 supports and a rigid frame ③ connected to the lever arm, two 100×100×500 mm prismatic
212 concrete specimens were loaded in a four-point bending configuration with a distance of 460
213 mm between the lower supports and 175 mm between the upper supports. The specimens,
214 which were placed in a thermally insulated box to minimize the impact of an accidental
215 variation of temperature, were tested simultaneously. In bending, concrete creep causes

216 deflection. If creep in tension and in compression were different, a displacement of the neutral
217 axis would also be observed. In order to characterize this behaviour, at least two
218 measurements were necessary. Therefore, strain was measured with strain gauges on the
219 upper and lower sides of the beam and on the initial neutral axis on each specimen. The strain
220 monitoring system used for the flexural test was the same as the one used in direct tensile
221 tests.

222 **IV Experimental results**

223 **IV.1 Modulus of elasticity upon creep loading**

224 The loading was applied quasi-instantaneously at the beginning of the creep test in order to
225 avoid both dynamic and time-dependent effects in the apparatus and in the specimen [25].
226 During loading, the material first underwent instantaneous (elastic) strain followed by viscous
227 strain. The Young's modulus of concrete could be calculated from the stress applied and the
228 instantaneous strain measured. Table 3 summarizes the different values of modulus of
229 elasticity obtained in direct tension, compression and bending for the three different loadings
230 (each value is the mean Young's modulus obtained on two specimens, with the corresponding
231 deviation in brackets). The applied stresses were equal to 30, 40 and 50% of the strength in
232 tension f_t for the tensile and flexural creep tests and 30, 40 and 50% of the strength in
233 compression f_c for the compressive creep. The moduli of elasticity were calculated upon
234 loading and at the end of the creep experiments, after removal of the load. The modulus
235 values obtained during conventional compressive tests as recommended by RILEM [38] are
236 presented in Table 2.

237 The Young's modulus values range between 40,610 and 45,610 MPa for all specimens upon
238 loading. Taking into account the scattering due to measurement inaccuracies and concrete
239 heterogeneity, the differences between the moduli at loading appeared to be small for the
240 three batches and the three types of loading. These values were not significantly different
241 from the Young's modulus obtained during a conventional strength test [38]. The loading
242 intensity did not affect initial stiffness, which indicates that the mechanical behaviour was
243 quite linear for a stress level ranging up to 30 to 50% of the compressive or tensile strength.
244 After removal of the load, an increase in stiffness could be observed for all specimens, except
245 for the batch corresponding to compressive creep at 30%. It may have been caused by the

246 effect of material ageing due to continuing hydration of anhydrous cement grains or by a
247 consolidation effect of the material due to creep [19, 39].

248 **IV.2 Results of creep measurements**

249 The aim of this study was to assess the effect of the stress level (applied stress / quasi-
250 instantaneous strength ratio) on compressive creep and tensile creep. The stress levels were
251 chosen between 30% and 50% of the compressive or tensile strength because the mechanical
252 behaviour is assumed to be linear in this stress range and, in practice, civil engineering
253 structures are subjected to stress levels close to such values. The precise values of stress levels
254 are difficult to know, especially in the case of tension, because of larger variability
255 characterizing the concrete tensile strength. Moreover, sustained loading could impact the
256 material microstructure [19, 40] and thus affect the material strength and the actual stress
257 level.

258 The total strains (including instantaneous strain, creep and shrinkage) obtained during tests in
259 compression, direct tension and flexure the same concrete mixture are plotted in Figure 5-a
260 and b, Figure 5-c and d, and Figure 5-e and f respectively. In the adopted sign convention, the
261 tensile strains (extensions) were considered positive, while the compressive strains
262 (contractions) were assigned the negative sign. Strains first increased in magnitude during the
263 early days, regardless of the type of loading. These findings are in agreement with usual
264 observations on short-term basic creep and can be explained by the micro-diffusion of water
265 under stress from the smaller pores to the capillaries. Differences in behaviour occurred after
266 about five days:

- 267 - **Direct compression loading:** the strain kinetics was first very fast, then decreased
268 slightly but remained significant even after 200 days of loading (Figure 5-a and b).
- 269 - **Direct tension loading:** the strains decreased regardless of load intensity (Figure 5-c
270 and d). The strain slope was different for the two specimens tested at 30% of the
271 tensile strength even though they came from the same batch and were subjected to the
272 same load (Figure 5-c). Such a difference was not observed with the specimens loaded
273 at 50% of the tensile strength (Figure 5-d).
- 274 - **Bending loading:** flexure-induced compression showed the same evolution as in
275 direct compression (Figure 5-e and f); the total strains measured on the stretched parts
276 of specimens (positive curves in Figures 5-e and f) did not have a significant negative
277 slope as observed for direct tensile tests, but rather stabilized.

278 Compressive creep results exhibited irreversible behaviours (with residual deformation). For
279 the tensile creep (direct tension and flexure-induced tension), strains became negative after
280 the total removal of the load.

281 All these observations highlight the very important role of shrinkage on creep and recovery in
282 tension. Shrinkage causes negative strain as compressive creep and thus has effects that
283 oppose tensile creep. Moreover, shrinkage is comparable in magnitude to tensile creep. The
284 analysis of the creep results has to take the influence into account.

285 **V Analysis and discussion**

286 **V.1 Specific basic creep**

287 Specific creep results (obtained after deducting instantaneous strain and shrinkage strains
288 presented in Figure 1) in direct tension, in compression and in bending have been plotted in
289 Figure 6 for the three stress levels.

290 Typical compressive creep curves exhibiting high initial kinetics were obtained (Figure 6-a).
291 The results show that compressive creep depends on load level: for two different stress-
292 strength ratios, namely 30% and 50%, compressive creep strains diverge from each other after
293 a few days of loading. For the HPC mixture studied in this paper, non-linearity apparently
294 occurs between 30 and 50%.

295 Tensile creep strains were expected to be small [21-23] and of the same magnitude as
296 shrinkage strains. In order to analyze such results, it was necessary to obtain shrinkage strains
297 for stress-free specimens in the same curing conditions as for loaded specimens. Each
298 specimen in tensile creep was associated with a control stress-free specimen (same shape,
299 same size and cast in the same batch in order to minimize scatter). Both specimens were kept
300 in the same thermally insulated box. Shrinkage strain was measured on the control specimens
301 with gauges identical to the ones used for the loaded specimen. The shrinkage subtracted to
302 the total strain of each specimen was the mean of the two measurements performed on the
303 control specimen. This way of superposing creep and shrinkage is a common approach that
304 assumes that the shrinkage of a loaded specimen is equal to the shrinkage of an unloaded one
305 [3, 41]. Tensile basic creep curves (obtained after the deduction of shrinkage strains) evolved
306 practically in the same way as compressive creep with high creep rates during the first five
307 days regardless of the stress level (Figure 6-b). After about 10 days, five specimens started
308 shrinking while the shrinkage strains measured on the control stress-free specimens have been

309 subtracted. The results were more scattered than for compressive creep and no specific trend
310 was found with regards to the stress level. It is important to note that the scatter of strain
311 measurement is quite small between two gauges stuck on a same specimen and mainly due to
312 small flexural moment during loading (the deviation between two gauges appeared at the
313 beginning of the test with little evolution during the creep tests – Figure 5-c and d). Moreover,
314 the same gauges were used for bending creep tests which present smaller dispersion (Figure
315 6-c). Therefore, the scatter was not mainly caused by the measurement system. Scatter of
316 tensile creep strain appears between different specimens and can be explained by usual
317 scattering of concrete response in tension. Concrete properties are usually more scattered in
318 tension than in compression (Table 2) and than in bending. It can explain why tensile creep is
319 more scatter than compressive and bending creep. The dispersion of the results can be
320 explained by three main factors: the very low magnitude of measured strains, the dispersion of
321 the concrete shrinkage strains and the dispersion of the direct tensile strength. First, the
322 scatters observed for the direct tensile creep results and for the autogenous shrinkage are
323 comparable in magnitude. Secondly, it is difficult to evaluate the stress level precisely in
324 tension because of the large dispersion of the direct tensile strength results (Table 2). The
325 stress level could thus be overestimated or underestimated. As creep is sensitive to stress
326 level, the effects on the measured creep strains could be significant.

327 For the flexural creep test, creep measured in the compression area and the one in the tension
328 area presented similar evolutions: high early rate of deformations and strains consistent with
329 the type of stress (Figure 6-c). The specific creep strains in flexure-induced tension (obtained
330 after deduction of the shrinkage strains measured on the control specimens) were positive
331 throughout the experiments, unlike the creep strains obtained in direct tension. While the
332 shrinkage was quite identical for the control specimens associated with the tension and with
333 the flexural tests, the consequence for the creep is not the same: a negative slope was noticed
334 for the tensile creep while a positive slope was observed for the flexural creep. Creep strain
335 curves were practically symmetrical in flexure-induced compression and tension for the 40%
336 and 50% stress levels (Figure 6-c), but not for the 30% level.

337 **V.2 Creep recovery**

338 The results of creep recovery in compression, in direct tension and in bending are presented in
339 Figure 7. Metrological problems prevented to record the recovery for the 30% loading level in
340 direct compression and bending. Creep recovery recorded under the different types of loading
341 (compression, tension, flexure) did not exhibit significant discrepancies when various types of

342 loading (tension, compression, bending) were considered, unlike the observations made by
343 Brooks and Neville [21], who reported differences between direct tension and direct
344 compression.

345 **V.3 Limit of the superposition of basic creep and of autogenous shrinkage strains**

346 Direct compressive creep results exhibited a usual trend. The non-linearity between 30 and
347 50% of ultimate strength can be explained by the dependence of basic creep on the density of
348 microcracks occurring during the creep test, as already observed and explained in [23,41]. In
349 the case of direct tensile creep, the experimental results can be considered as unexpected, with
350 most of the specimens exhibiting a tendency to ‘contract’ after a few days under load (Figure
351 6-b). However, the shrinkage strains measured on the control specimens have already been
352 deducted from the total strains (assuming that the hydration evolution is the same for a
353 specimen loaded and unloaded one) and thus the contraction cannot be explained by the usual
354 shrinkage due to regular continuous hydration. The slope of contraction for all the specimens
355 in tension is low (less than $-0.1 \mu\text{m}/\text{m}/\text{MPa}/\text{day}$). However, it is important to remind the
356 particular attention paid to obtain representative shrinkage strain with the association of one
357 stress-free specimen for each loaded specimen. It must also be noted that tensile creep curves
358 of five (on the six) specimens tested in tension present negative slopes while all the flexural
359 tensile creep curves obtained in the same conditions with the same measurement tools exhibit
360 positive slopes. Even if the negative slope is small, the result appears to be systematic and
361 could have a physical explanation other than the only uncertainty of the shrinkage
362 measurement.

363 Such results had already been reported by Reinhardt and Rinder for basic creep at high
364 loading levels on high performance concrete loaded after 28 days [28]. As already explained
365 by these authors, the increase in creep cannot be negative. It implies that the shrinkage of
366 loaded specimens may be greater than the shrinkage obtained on control, stress-free samples.
367 When concrete is loaded, it will crack even at a stress levels lower than 20% in direct tension
368 [26]. According to Rossi et al. [23], these cracks could generate a brutal internal hydric
369 imbalance resulting in a phenomenon similar to drying which causes additional shrinkage.
370 Cracks could also cross anhydrous grains of the cement paste and increase their hydration
371 kinetics. This continuation of hydration would induce further autogenous shrinkage and could
372 partially compensate damage and even lead to an increase in strength. This is in accordance
373 with Reinhardt and Rinder’s observations pointing out that the relative humidity decreased
374 more in the loaded specimens than in the stress-free specimens during basic tensile creep

375 experiments [28]. It can be concluded that the more microcracked the concrete is, the greater
376 the additional shrinkage strain will be. This interaction between the two phenomena is similar
377 to the Pickett effect demonstrated for the creep of concrete in compression [25, 42, 43].
378 Indeed, this effect has been explained through the role of skin cracking and of the decrease of
379 humidity [25]. For specimens in tension under stress level lower than 50% of the tensile
380 strength, the creep loading does not cause localized cracks and the subsequent failure.
381 However, the instantaneous loading could cause damage as observed with acoustic
382 measurements or with ultrasonic pulse velocity techniques in [27, 44-45]. Using these non-
383 destructive techniques, authors reported that the first damages were detected from 30% of
384 tensile strength. Moreover, microcracks have been detected for creep test at stress level of
385 30% of the strength and it has been noticed that creep strains is proportional to the number of
386 microcracks created in the material [23, 41]. As a consequence, creep is associated to damage.
387 Notwithstanding the propagation of microcracks could be limited by the presence of voids or
388 aggregates. In that case, induced damage could have a less effect on mechanical properties
389 than the continuous hydration of cement and could not be detected at unloading. In such
390 conditions, during the tensile creep tests, damage would not lead to increase the strain due to
391 localized cracks. However it could be sufficient to cause additional contraction strains due to
392 the decrease of humidity (due to continuation of hydration) as for the Pickett effect. Even
393 small damage and consequences on shrinkage could cause the variation of capillary
394 depression necessary to induce additional shrinkage which could explain the observed
395 negative slope.

396 In this analysis, the strain recorded during the flexural creep tests contributes additional
397 information. In the bending creep tests, only a small fraction of the volume is loaded up to the
398 nominal stress level. The measured compressive strength was about 20 times larger than the
399 tensile strength. The compressed zone in the bending specimen was thus loaded at a level less
400 than 2% of the compressive strength. In the tension zone, only the lowest portion (extreme
401 fiber) of the beam was really loaded at the nominal stress level. Although the cross-section
402 remained plane [46-47], only a fraction of the specimen height was subjected to a really high
403 stress rate. In bending tests, the average stress level over the cross section is less than 50% of
404 the nominal stress, thus restricting damage. Moreover, the non-uniformity of the stress and
405 strain fields in flexure specimens contributed to stable microcracking control. It allowed
406 larger local deformations than in a uniform field case without unstable propagation of cracks
407 [48]. Consequently, the additional cracking-induced shrinkage was no longer significant,

408 explaining why the curve slopes corresponding to creep strains in direct tension and bending-
409 induced tension were not identical (Figure 6-b and c). In flexure, creep strains appeared to be
410 the same in flexure-induced compression and in bending-induced tension as already observed
411 for direct tension and compression performed in water [21]. In this case, the effect of
412 shrinkage on concrete is probably cancelled or at least largely reduced. No significant
413 differences were observed for the three loading levels and basic creep appeared to be fairly
414 linear in flexural creep (flexure-induced tension and flexure-induced compression) between
415 30 and 50% of the tensile strength, in contrast with the non-linearity observed for compressive
416 creep (Figure 6).

417 While basic creep appears to be different in tension, in bending and in compression, the
418 recovery in the direct tensile creep experiments was roughly the same as in bending and
419 compression. As a consequence, the reversible part of creep appears to be the same for the
420 three loading modes and the difference of basic creep should possibly be searched in the
421 irreversible part of creep for which damage plays a prominent role. But it also means that
422 during recovery, shrinkage was quite the same for all the specimens. If shrinkage strains were
423 really modified for loaded specimens compared to stress-free specimens (perhaps in
424 interaction with damage), probably due to the closure of microcracks this effect stopped when
425 the specimens were unloaded. On-going experimentations with longer recovery period will
426 allow these points to be clarified.

427 **V.4 Comparison of tensile, compressive and flexural basic creep**

428 The specific basic creep in compression, in tension and in bending obtained after deducting
429 instantaneous strain and shrinkage strain (presented in Figure 1) is plotted in Figure 8. To
430 make comparison easier, absolute values of creep strains have been used. During the first few
431 days of loading, creep strains did not appear to be significantly different, whatever the type of
432 loading (direct tension, compression, flexure-induced tension or flexure-induced
433 compression). All strain curves evolved in accordance with the loading conditions. Tensile
434 creep data recorded in direct tension and flexure creeps were quite similar (between 3 and 5
435 $\mu\text{m}/\text{m}/\text{MPa}$) for all the specimens, whatever the stress level, while compressive creep was
436 twice as large (between 7 and 9 $\mu\text{m}/\text{m}/\text{MPa}$).

437 After 5 days, quite a clear partition appeared: compressive creep strains were the largest,
438 flexure-induced tension and flexure-induced compression were intermediate, while tensile
439 creep strains were the smallest and began to decrease after 5 to 10 days of testing (Figure 8).

440 Compressive creep was the largest, but the results obtained for the 30% stress level were not
441 significantly larger than those recorded in flexure. Two specimens in direct tension (taken to
442 be loaded at 30 and 40% of the tensile strength) exhibited creep strains quite close to the creep
443 obtained in flexure, while the other four exhibited negative strains after 5 or 10 days of
444 loading. As explained above, flexural creep should be less affected by the coupling between
445 damage and shrinkage. It could thus be expected to obtain flexural creep strains in between
446 the compressive creep strains (which could be increased by the coupling with shrinkage) and
447 the tensile creep strains (which could be decreased by the coupling with shrinkage), as
448 observed in Figure 8. The difference between direct tensile creep and flexural tensile one
449 appears to be systematic and could be explained by the impact of microcracking on shrinkage
450 strains. However, experimental evidence of damage had not been obtained on the specimens
451 studied. Additional tests are required in order to determine and to quantify the potential effect
452 of microcracking on shrinkage and subsequent effect on the creep behaviour of the material.

453 **VI Conclusion**

454 Few studies have been devoted to tensile creep of concrete, particularly for concrete older
455 than 28 days, i.e. when hydration reactions are almost stabilized. In the field, sound
456 comparisons with compressive creep are scarce. This contribution presents the results of a
457 comparative study focusing on creep in different modes of loading: direct tension, direct
458 compression and flexure. Basic creep test results obtained under these different types of
459 loading have been analysed and compared for three stress levels. For this purpose, specific
460 devices devoted to tensile and to flexural creep were developed. Results show that the
461 behaviour depends on the type of loading. It is unnecessary to specify that a realistic modeling
462 of concrete response requires knowledge of the creep under these different types of loading.
463 During experiments, attention was paid to avoid artifacts that could be induced by thermal
464 variations. Shrinkage strains were measured with great care and high accuracy.

465 In terms of stress levels, non-linearity was found for compressive creep to arise somewhere
466 between 30 and 50% of the compressive strength for the HPC studied. For direct tension tests,
467 the tensile strength variability made it difficult to conclude, and for flexure creep, the loading-
468 induced damage appeared to have limited effects in the stress level range investigated
469 (between 30 and 50% of the tensile strength).

470 Shrinkage plays an important role in the estimation of creep and analysis is made difficult due
471 to the low strains magnitude, the dispersions of the shrinkage strains and uncertainty on the
472 tensile strength of the concrete. In spite of these difficulties, the differences between direct
473 tensile creep, compressive creep and flexural creep measured in this work are systematic. The
474 assumed superposition of basic creep and autogenous shrinkage could be relevant only if the
475 specimen did not undergo significant damage (flexural test at stress levels equal or lower than
476 50% for the tests performed in this study). Initiation of first microcracks in the case of
477 uniform loading (direct tension or compression) made the interpretation of results complicated
478 due to the strong interaction between shrinkage and damage. Such interaction could increase
479 the shrinkage strain of the loaded specimens compared to the shrinkage of control specimens
480 (stress-free specimens). The recovery appears to be the same for the three modes and the
481 differences of basic creep for the three loading modes should probably be sought in the
482 irreversible part of creep. The conventional assumption that the two phenomena can simply be
483 superimposed ceases to be valid. Such assumption would lead to overestimate the basic creep
484 in compression and underestimate the basic creep in direct tension. The main problem in
485 analysing the behaviour of concrete under sustained loading in tension and in compression is
486 then to quantify the relation between shrinkage and damage. This should be done through
487 complete modelling that enables such coupling to be considered. It is the purpose of the
488 current phase of the undergoing research program. On-going experiments are focusing on
489 quantification of this damage due to low stress levels on the magnitude of shrinkage strain.

490 **VII Acknowledgments**

491 This work was carried out at LMDC Toulouse with financial support from Andra in the
492 framework of a group of ‘cementitious materials structures behaviour’ research laboratories.

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609 **TABLES**

610 Table 1: Composition of concrete mixture

Composition of concrete in kg/m³	
<i>Cement CEM I 52.5R PM-ES (Val d'Azergues), Lafarge</i>	400
<i>Limestone sand 0/4 mm, Boulonnais</i>	858
<i>Limestone aggregate 4/12.5 mm, Boulonnais</i>	945
<i>Superplasticizer Glénium 27, MBT</i>	2.2
<i>Total water</i>	178

611

612 Table 2: Mechanical properties at 28 days (CV: coefficient of variation)

Batch	Tension			Compression			Modulus in compression		
	Mean (MPa)	CV	Tested samples	Mean (MPa)	CV	Tested samples	Mean (MPa)	CV	Tested samples
B-30%	3.48	19%	6	74.6	1.7%	2	42040	2.4%	3
B-40%	3.59	10%	8	67.5	2.6%	6	40610	2.9%	4
B-50%	2.99	13%	10	73.5	4.0%	6	41705	1.8%	4
All batches	3.31	16%	24	71.1	5.4%	14	41438	2.8%	11

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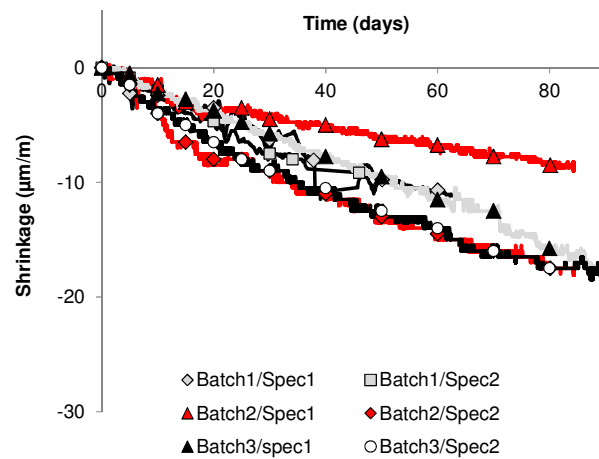
616 Table 3: Instantaneous elastic modulus upon loading and after unloading (in MPa – the values
617 are the mean obtained on two specimens, maximal deviation compared to the mean value is
618 given in brackets, fc and ft stand for compressive and tensile strengths respectively)

	At loading			After unloading		
	30% fc or ft	40% ft	50% fc or ft	30% fc or ft	40% ft	50% fc or ft
Compression	45610 (4350)		44570 (5460)	41885 (250)		53235 (14250)
Tension	41215 (415)	44300 (345)	43740 (625)	42160 (340)	46850 (770)	45375 (1010)
Bending	44065 (0)	42655 (1275)	44810 (2005)		44290 (1030)	47670 (2270)

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620 FIGURES

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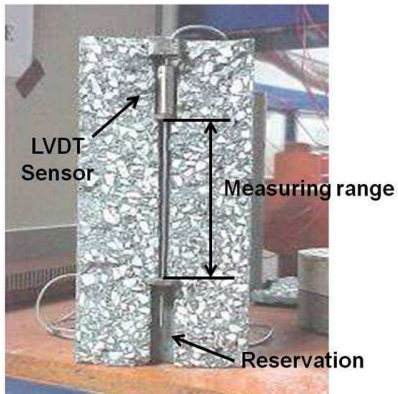


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623 Figure 1: Shrinkage strains for specimens kept in an insulated box from 28 days after the
624 casting. For each batch, results for two different sizes of specimen (Spec1 correspond to
625 70×70×280 mm prisms and Spec2 to 100×100×500 mm prisms) are presented.

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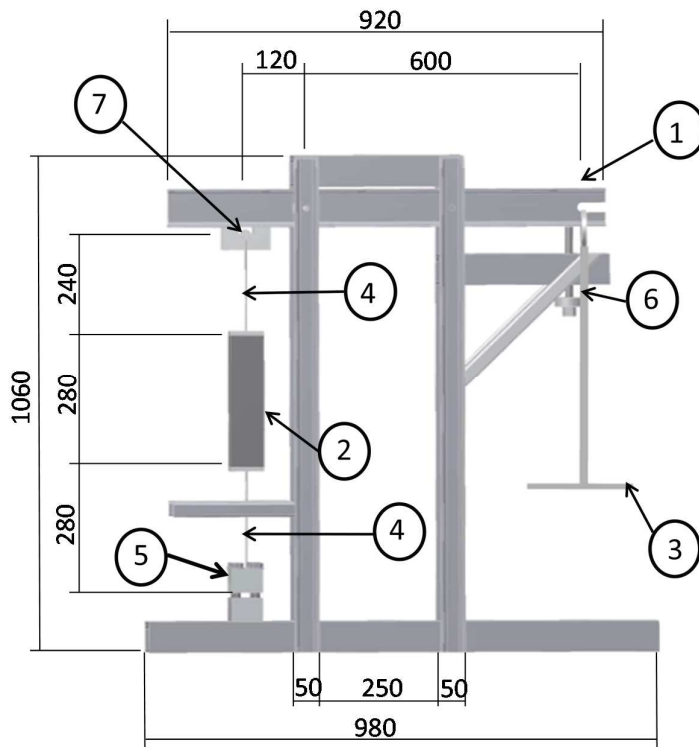
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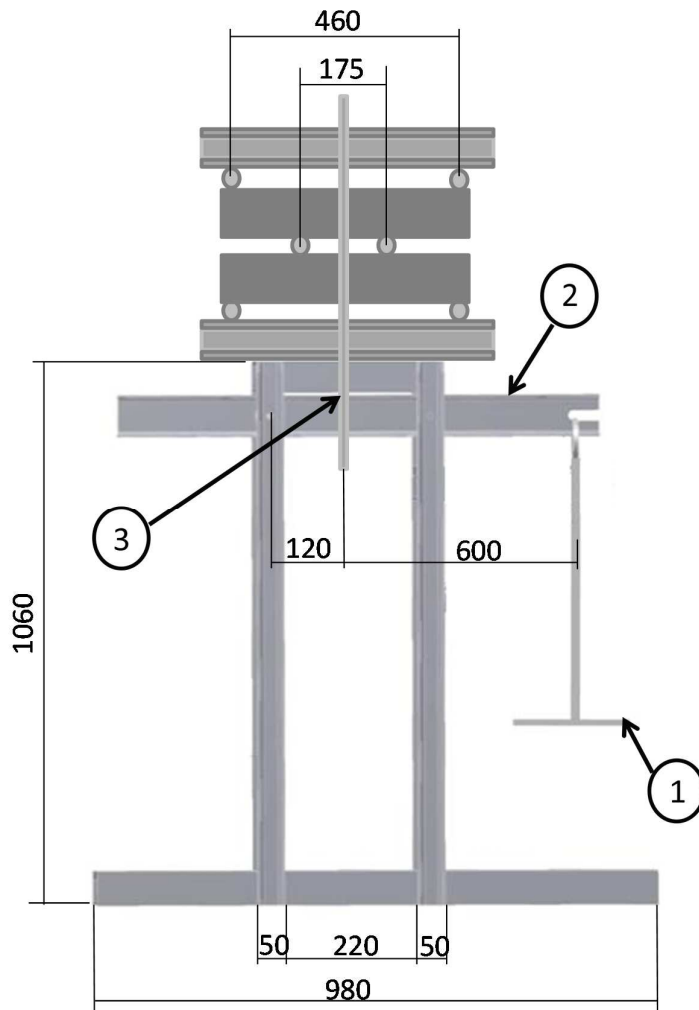
629 Figure 2: Longitudinal measurement for compressive creep test (inductive transducer in the
630 reservation)

631



632

633 Figure 3: Tensile creep device (① lever arm, ② 70×70×280 mm prismatic specimen, ③
634 platen, ④ cable, ⑤ screw system to control the horizontality of the lever arm, ⑥ stopping
635 device, ⑦ cylindrical roller).

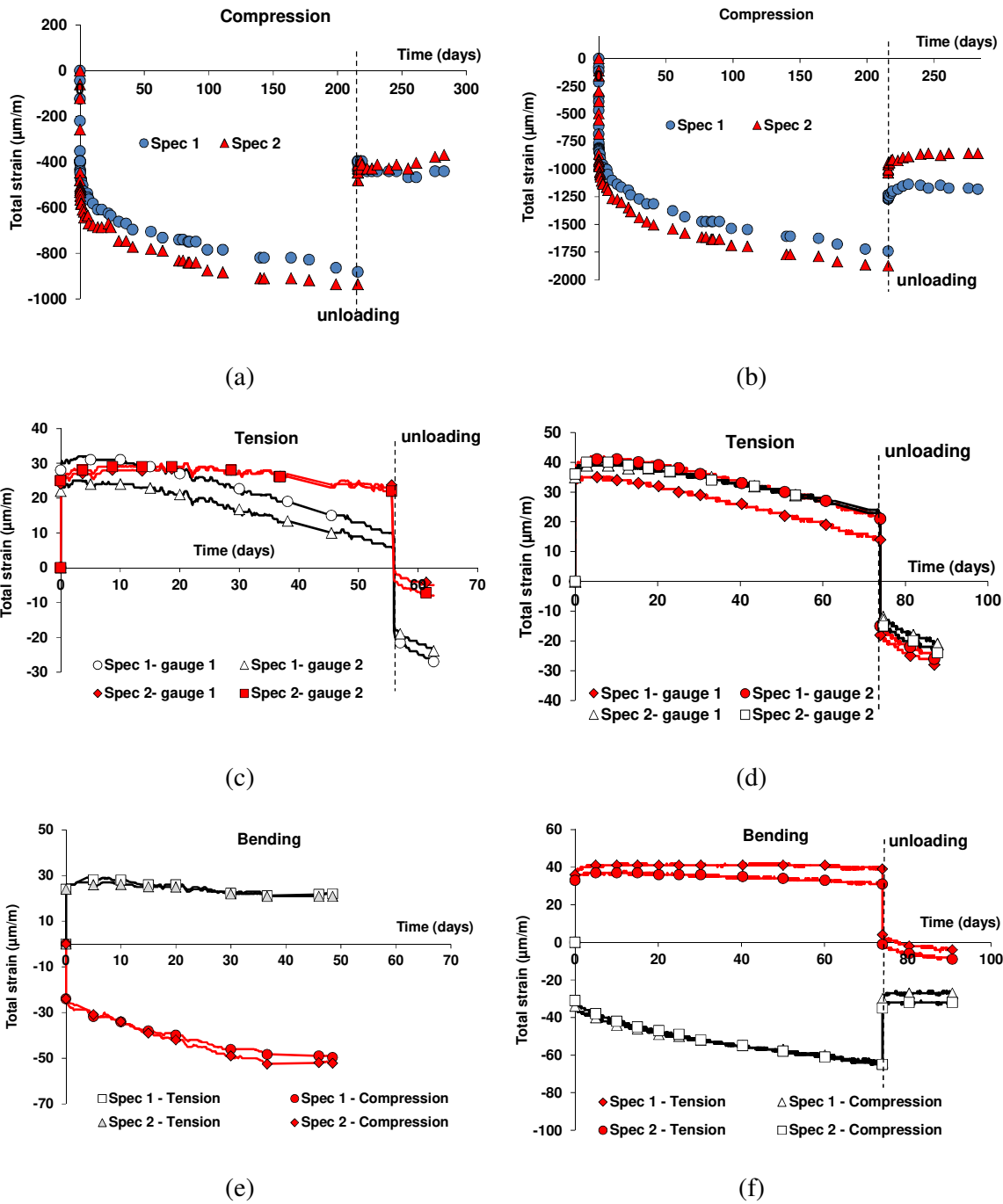


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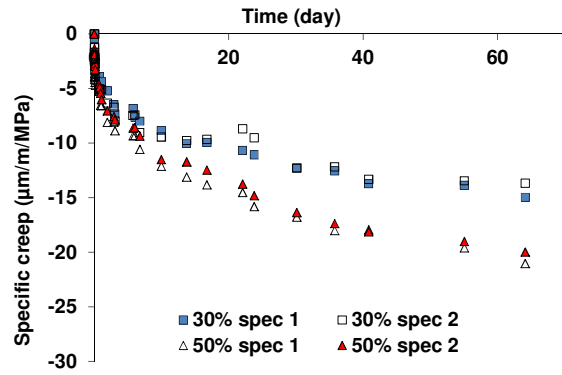
637 Figure 4: Flexural creep device (① platen, ② lever arm, ③ rigid frame to ensure the
638 transmission of the loading from the lever arm to the specimens)

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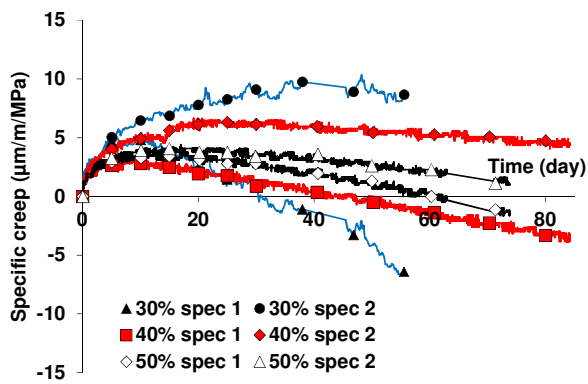
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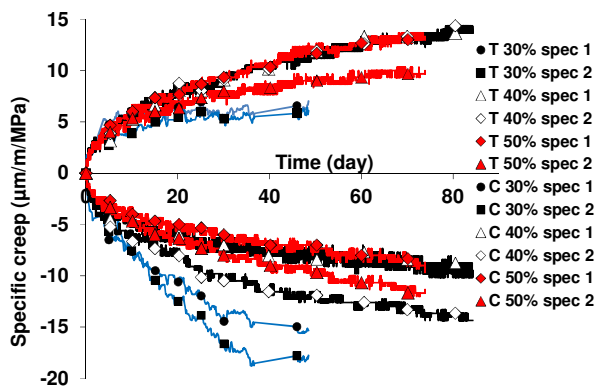
642 Figure 5: Total strains (elastic strains included) in compression at 30% and 50% of f_c (a and
 643 b), in tension at 30% and 50% of f_t (c and d), and in flexure at 30% and 50% of f_t (e and f)



(a)

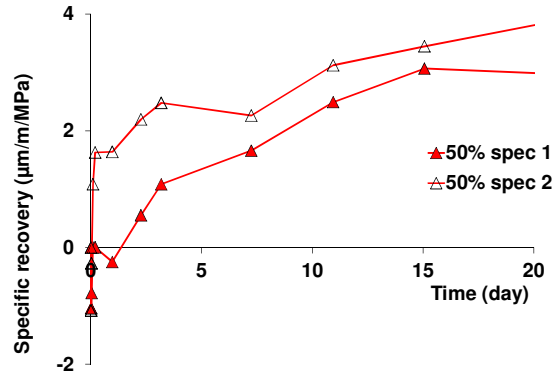


(b)

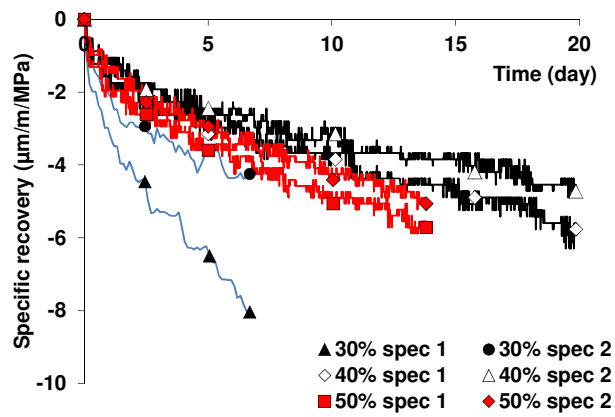


(c)

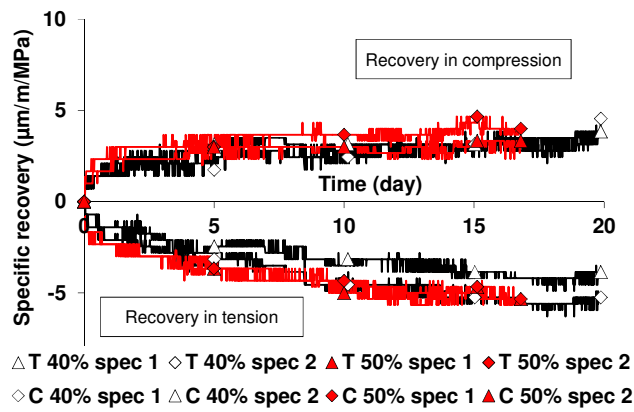
645 Figure 6: Specific creep in compression (a), in tension (b) and in flexure (c)



(a)



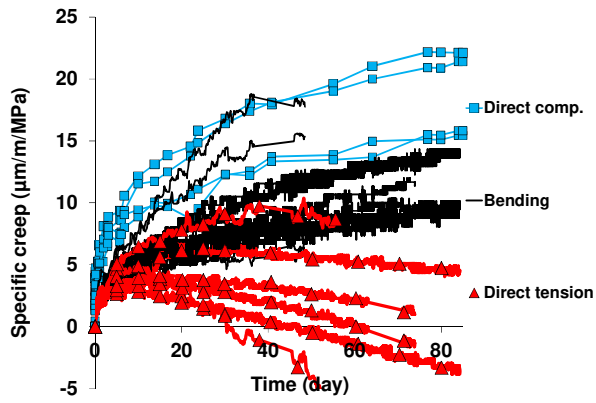
(b)



(c)

646 Figure 7: Specific recovery in compression (a), in tension (b) and in flexure (c)

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648

649 Figure 8: Comparison of direct tensile creep, direct compressive creep and flexural creep in
 650 terms of specific basic creep (for the three stress levels)

651